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Relations & Functions

Relation: A set of ordered pairs or pairing of input values with output values.

Domain: The set of input values.

Range: The set of output values.

Representing Relations:

A relation can be represented in the following ways.

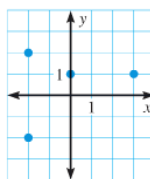
Ordered Pairs

- (-2, 2)
- (-2, -2)
- (0, 1)
- (3, 1)

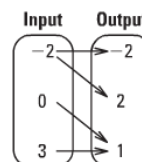
Table

x	y
-2	2
-2	-2
0	1
3	1

Graph



Mapping Diagram

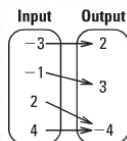


In each case the domain is $\{-2, 0, 3\}$ and the range is $\{-2, 2, 1\}$

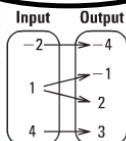
Some relations are functions.

A **function** is a relation for which each input has exactly one output. If any input of a relation has more than one output, the relation is *not* a function.

Function



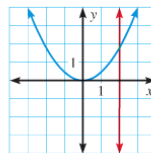
~~Function~~



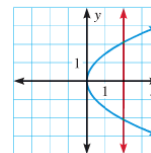
The vertical line test:

A relation is a function if and only if no vertical line intersects the graph of the relation at more than one point.

Function



Not a function



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Equations in Two Variables

EQUATIONS IN TWO VARIABLES Many functions can be described by an **equation in two variables**, such as $y = 3x - 5$. The input variable (in this case, x) is called the **independent variable**. The output variable (in this case, y) is called the **dependent variable** because its value *depends* on the value of the input variable.

In this case....

$x = \text{input} = \text{independent variable} = \text{domain}$

$y = \text{output} = \text{dependent variable} = \text{range}$

$f(x)$ does not mean multiply f by x !!!!!!!!!!!

Linear Equations: $y = mx + b$

Linear Functions: $f(x) = mx + b$

Function
Notation

$f(x)$ means the output value of the function when the input value is the number x .

For example $f(8)$ means the value of the function evaluated for an input value of 8.

For $f(x)$ we say, "f of x." For $f(8)$, we say, "f of 8."

$$y = 3x - 5$$

$$f(x) = 3x - 5$$

$$f(8) = 3(8) - 5$$

$$f(8) = 19$$

p. 76/ # 1, 7 - 11, 16, 17, 21-23, 29 - 31, 34 - 36, 44 - 47, 51, 55, 61

due Wednesday